

1. Evaluate the following surface integrals of scalar fields.
 - a. $\iint_S (z + 2x + \frac{4y}{3}) dS$, where the surface S is the part of the $6x + 4y + 3z = 12$ plane which lies in the first octant.
 - b. $\iint_S x dS$, where S is the part of the sphere of radius 3 and center at the origin which lies in the first octant.
2. Evaluate $\iint_S f(x, y) dS$, where the scalar field $f(x, y) = x\sqrt{y^2 + 1}$ and S is the surface cut from the paraboloid $y^2 + 4z = 16$ by the planes $x = 0$, $x = 1$ and $z = 0$.
3. Find $\iint_S (x\mathbf{i} + y\mathbf{j} + z\mathbf{k}) d\mathbf{S}$, where S is that part of the paraboloid $z = x^2 + y^2$ that lies above the circle $x^2 + y^2 = 4x$, oriented so that the normal points outward.
4. Find $\iint_S (x\mathbf{i} + y\mathbf{j}) d\mathbf{S}$, where S is that part of the sphere $\mathbf{r}(u, v) = 4\{\cos u \cos v, \cos u \sin v, \sin u\}$ for which $v \leq u \leq \frac{\pi}{2}, 0 \leq v \leq \frac{\pi}{2}$ and oriented so that the normal points outward.
5. Evaluate the surface integral $\iint_S \mathbf{F}(x, y, z) d\mathbf{S}$, oriented so that the normal points upward, where
 - a. $\mathbf{F}(x, y, z) = (x - 2z)\mathbf{i} + (2x + y)\mathbf{j} + (x - y + z)\mathbf{k}$ and the surface S is the upper half of the sphere of radius 2 and center at the origin.
 - b. $\mathbf{F}(x, y, z) = xy\mathbf{i} + (x + z)\mathbf{j} - 2y^2\mathbf{k}$ and S is the surface cut from $z = \frac{y}{x}$ by the planes $y = -x$, $y = x$, $x = 1$ and $x = 2$.
 - c. $\mathbf{F}(x, y, z) = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$ and S is that part of the surface $\mathbf{r}(u, v) = \{(3 + \cos u) \cos v, (3 + \cos u) \sin v, \sin u\}$ that lies above the xy -plane.
 - d. $\mathbf{F}(x, y, z) = yz\mathbf{i} - xz\mathbf{j} + z\mathbf{k}$ and S is that part of the surface $\mathbf{r} = \{u \cos v, u \sin v, 2v\}$ for which $0 \leq u \leq 1, 0 \leq v \leq 2\pi$.
 - e. $\mathbf{F}(x, y, z) = -xy\mathbf{i} + xy\mathbf{j} + z\mathbf{k}$ and S is that part of the surface $z = x^2 - y^2$ that lies above the square $\{(x, y); -2 \leq x \leq 2, -3 \leq y \leq 3\}$.
6. Find the flux of $\mathbf{F}(x, y, z) = x\mathbf{i} + z\mathbf{j}$ out of the tetrahedron bounded by the coordinate planes and the plane $2x + 3y + 4z = 12$.

7. Find the flux of $\mathbf{F}(x, y, z) = 2x\mathbf{i} + 4y\mathbf{j} + 3\mathbf{k}$ outward through the surface cut from the bottom of the paraboloid $z = x^2 + y^2$ by the plane $z = 2$.